

# Drones for Last-Mile Delivery

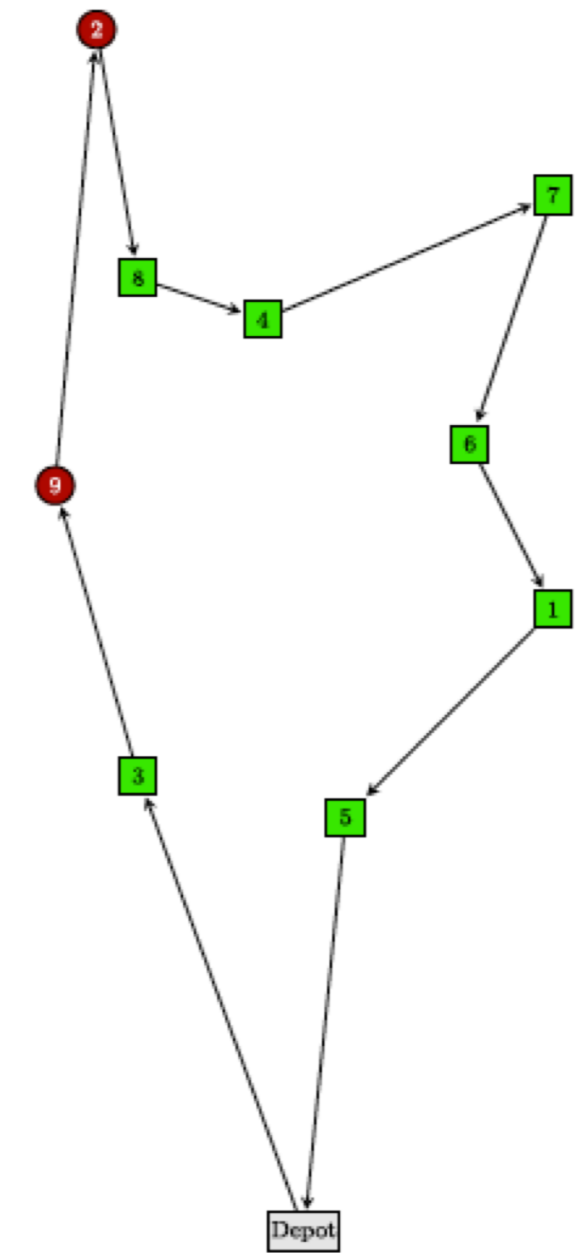
## Motivation / Background

### Background:

- Global parcel delivery market valued at \$82 bn and expected to double in next decade (McKinsey, 2016).
- Last mile makes up greater than 50 percent of market costs.

### Immediate benefits with drones:

- Significantly cut variable costs by cutting fuel and labor.
- Faster delivery of products due to higher travel speeds.



(a) An optimal truck delivery sequence, without the aid of a UAV.

## Key Question / Hypothesis

Under what conditions will the integration of drones into last-mile delivery make sense?

## Relevant Literature

2015 – Murray and Chu, The flying sidekick traveling salesman problem: Optimization of drone-assisted parcel delivery. *Transportation Research Part C: Emerging Technologies*, 54:86-109.

2016 – McKinsey & Company, Parcel Delivery: The Future of Last Mile.



Prime Air – UK – 2013

amazon.com

## The Problem

Physical Limitations	Operational Strategy	Government Regulation
Drones have a max payload of 5 lbs and limited range of 10 mi.	A complete solution defining drone delivery execution has not been fully developed.	Current laws in US require line of sight and 400 ft ceiling.

## Methodology

- Vehicle Routing Problem
- Mixed Integer Linear Programming
- Approximate Solutions with Heuristics

## Initial Results

### Objective Function:

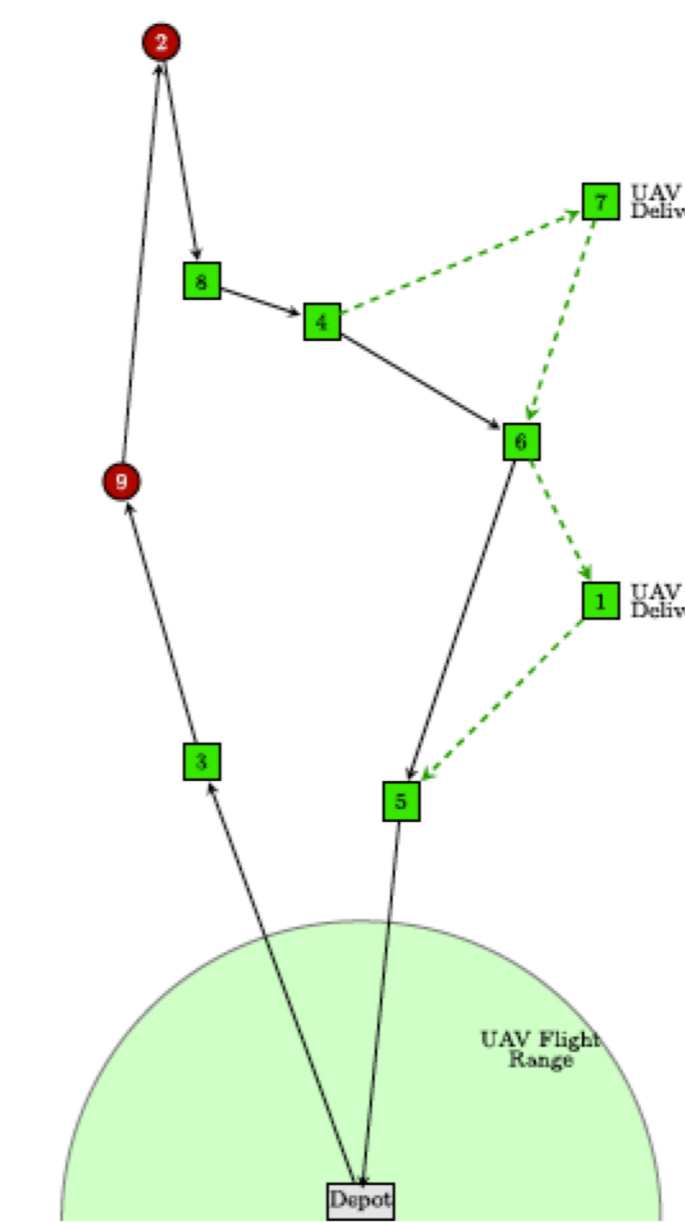
Min Cost =

$$\underbrace{\sum_i \sum_j x_{ij} t_{ij} c_t}_{\text{Truck}} + \underbrace{\sum_i \sum_j \sum_k \sum_n y_{ijkn} c_d (t_{ij}^d + t_{jk}^d)}_{\text{Drone}} + \underbrace{\sum_n C_n z_n}_{\text{Drone Deploy}}$$

### Variables:

$x_{ij}, y_{ijkn}, z_n$  = Binary Decision Variables  
 $t_{ij}, t_{ij}^d, t_{jk}^d$  = Travel Time  
 $c_t, c_d$  = Variable Cost  
 $C_n$  = Fixed Cost per Drone Dispatch

## Expected Contribution



(b) The UAV is launched from a delivery truck, delivering parcels to two eligible customers.

### Develop algorithms to:

- Model and optimize drone operations as a function of cost.
- Model multi-drone deployment.
- Solve problems more efficiently with heuristic.

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